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Wall-Modeled Large Eddy Simulation of a Three-Dimensional Shock-Boundary Layer Interaction

THESIS

Nicholas J. Marco, 2d Lt, USAF AFIT-ENY-MS-18-M-277

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AFIT-ENY-MS-18-M-277

WALL-MODELED LARGE EDDY SIMULATION OF A THREE-DIMENSIONAL SHOCK-BOUNDARY LAYER INTERACTION

THESIS

Presented to the Faculty Department of Aeronautics and Astronautics Graduate School of Engineering and Management Air Force Institute of Technology Air University Air Education and Training Command

in Partial Fulfillment of the Requirements for the Degree of Master of Science in Aeronautical Engineering

Nicholas J. Marco, B.S.M.E., E.I.T

2d Lt, USAF

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Abstract

The computational cost of direct simulation of turbulent flows is prohibitive at high Reynolds numbers; thus, methods such as RANS and LES are used in order to model relevant engineering flows computationally. However, these methods require a large number of cells near a solid boundary increasing the computational time. To circumvent this issue, models that eliminate this need for large cell counts near solid boundaries can be used. One such method utilizes a Wall-Modeled Large Eddy Simulation (WM-LES). Of interest is how these wall models perform in comparison to a Wall-Resolved Large Eddy Simulation (WR-LES) and experimental results of a shock turbulent boundary layer interactions (STBLI) and specifically, whether equilibrium wall models are sufficient to resolve the oscillatory and hence non-equilibrium nature of these flows or whether a non-equilibrium model is necessary. To study this a swept compression ramp which produces a 3-D STBLI was simulated using a Wall-Modeled Large Eddy Simulation. It was found that an equilibrium model is insufficient in determining both large scale features such as separation and reattachment locations as well as specific flow quantities such as wall shear While a non-equilibrium model did better in predicting both large scale features and specific flow quantities. However, the non-equilibrium model produced a non-physical secondary reattachment leading to a need for further research into the specific model.



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Nicholas J. Marco



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List of Symbols

Symbol	Page
Re	Reynolds Number
У	Y-displacement
+	Wall-units
ϵ	Energy
ν	Kinematic viscosity
κ	Wavenumber
$u_{ au}$	Friction velocity
$ au_w$	Wall shear stress
ρ	Density
u	Streamwise velocity
κ	von Karman Constant
С	Integration Constant
vD	van Driest Transformed11
W	Value at wall
U	Vector of conserved variables15
F_{j}	Flux Vector
x_j	Direction indexing
u	Velocity in j-direction
Е	Total specific energy
р	Static pressure
δ_{ij}	Kronecker delta
σ	Viscous stress tensor



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Symbol

q	Heat conduction
R	Gas constant
Т	Temperature
γ	Ratio of specific heats16
S_{ij}	Rate of strain tensor
λ	Bulk viscosity
$\hat{\mu}$	Effecitve viscosity
$\hat{\kappa}$	Effecitve thermal conductivity16
μ	Molecular component of viscosity
μ_t	Turbulent component of viscosity
κ	Molecular component of thermal conductivity
κ_t	Turbulent component of thermal conductivity
\overline{U}	Filetered variable17
U'	Sub-filtered variable
G	Filter function
Δ	Filter width
Q	Wall-modeled vector of conserved variables
G	Wall-modeled flux vector
D	Damping function



WALL-MODELED LARGE EDDY SIMULATION OF A THREE-DIMENSIONAL SHOCK-BOUNDARY LAYER INTERACTION

I. Introduction

1.1 Study of Turbulent Flows

The turbulent nature of many flows of engineering interest is important due to the flows increased ability to transfer momentum. This increased transfer of momentum at a solid boundary, such as the surface of an aircraft, leads to higher values of quantities such as drag, heat transfer, and mass transfer. These quantities play major roles in the performance of aircraft and thus it is important for engineers to accurately predict such values[8]. Turbulence has a continuous range of energetic scales in both time and length, in which the largest scales are heavily influenced by the geometry of the flow whereas the smallest scales are determined by the rate at which they receive energy from the larger scales[8]. The continuous range of turbulent length scales, decreasing in size to a solid boundary, can be seen in Figure 1.

When studying turbulent flows, the use of experimental facilities is often limiting due to short run-times, restricting methods of data collection, and the inability to replicate the exact flight conditions of interest[5]. Alternatively, one can use Computational Fluid Dynamics (CFD) which solves the governing equations of fluid dynamics, the Navier-Stokes Equations, through discretization of the domain of interest. CFD can provide flexibility in the aforementioned areas which plague experiments such as reproducing exact flight conditions as well as the ability to obtain data from nearly



1



Figure 1. Turbulent boundary layer with contours of density. Direct numerical simulation of Pirozzoli and Bernadini[1]

any point in the flow. However, CFD present its own challenges, mainly: high computational cost for flows of engineering interest and the accuracy of models included in the numerics.

1.2 Simulation of Turbulent Flows

In order to simulate a turbulent flow with effectively no modeling, one would be required to use a Direct Numerical Simulation (DNS), which resolves all the scales of turbulence. However, DNS is extremely costly since the number of grid points needed to sufficiently resolve the smallest turbulent eddies scales as a function of the Reynolds number, $Re^{9/4}$ [9]. To circumvent this issue, turbulence models are used to model the smaller scales and therefore create a less costly computation. However, these models still require similar grid resolution requirements near solid boundaries, with a maximum height of the wall-adjacent cell limited to under one wall unit ($y^+ \leq 1$). Where, y^+ is a dimensionless wall distance of a wall-bounded flow. This limit is true of a Wall-Resolved Large Eddy Simulation (WR-LES). This clustering of small cells along the wall boundaries, or "near-wall problem," decreases the size of the timestep that can be used therefore limiting the Reynolds number that can be studied. This restriction poses a problem to studying flows of engineering interest at high Reynolds numbers, such as hypersonic flows or full vehicle simulations.



Traditionally, Reynolds-Averaged Navier-Stokes (RANS) methods, in which the mean flow is solved, are used in such high Reynolds number cases. However, these methods have been found to be erroneous in more complex flows, such as turbulent shock wave interactions, thus warranting the need for turbulent eddies to be resolved[10]. A possible solution to the inaccurate results of RANS and the high computational cost of wall-resolved LES is using a wall-model that approximates the energetic motions of the inner boundary layer, removing the need for a fully resolved grid near a wall[11]. This method is called Wall-Modeled Large Eddy Simulation (WM-LES). Without the restriction of small cells near the wall, larger cells and therefore larger timesteps can be used resulting in quicker computational times. With the added assumptions of using a wall-model one must first identify which flow features the specific wall-model is well suited to capture as well as where it is not appropriate to be used.

1.3 Shock Turbulent Boundary Layer Interactions

One such flow feature that is of interest to the academic community is Shock Turbulent Boundary Layer Interactions (STBLI). While the wall-modeled method has been used to predict Shock Turbulent Boundary Layer Interactions in two-dimensional flows with good accuracy, little research has assessed WM-LES of compressible flows with three-dimensional characteristics[12].

This study will simulate a flow with a three-dimensional STBLI, specifically a swept-ramp configuration, with a WM-LES. The accuracy of the wall-model in predicting certain flow properties, such as mean wall shear stresses and the location of the Virtual Conic Origin (VCO), will be determined by comparison to both a wallresolved and experimental study of the same configuration. The specific geometry chosen to produce these three-dimensional STBLI is a swept-compression ramp with



22.5° of compression and 30° of sweep. This specific ramp has previously recorded data from the WR-LES computations of Adler et al. and the experiments of Vanstone et al. for this study to compare to [2, 7]. This geometry can be seen in Figure 2.

Also of interest is comparison of the WM-LES to simulations run using other popular techniques of decreasing computational time. One such technique is the use of a hybrid RANS/LES method such as Delayed Detached Eddy Simulation (DDES), specifically, using the Catris-Aupoix compressible formulation of the Spalart-Allmaras one-equation turbulence model[13][14].

Conclusions will be drawn on the effectiveness of the current wall-model in predicting the dynamics of a three-dimensional STBLI as compared to the aforementioned studies to include prediction of: location of separation, reattachment, and VCO and values of wall shear, skin friction, wall heating, and spectral content. Specifically, the following research questions will be answered:

• Can a WM-LES adequately predict the dynamics of a three-dimensional shock turbulent boundary layer interaction generated by a swept-ramp?

Specifically:



Figure 2. A 30 degree sweep, 22.5 degree compression swept-ramp as presented by Adler et al.[2].



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- How does the location of flow features such as separation, reattachment, and virtual conic origin compare between the WM-LES, WR-LES, and experiment?
- How do mean flow quantities compare between the WM-LES, WR-LES, and experiment?
- What is the savings in computational time between the WM-LES and WR-LES?
- How do the WM-LES and WR-LES compare to simulations run using a hybrid RANS/LES method, such as DDES, for a three-dimensional shock turbulent boundary layer interaction?



II. Literature Review

There is a large amount of current research into methods of modeling turbulence that both accurately predict the physics of the phenomenon and greatly decrease the computational time needed to model such flows. Historically, the majority of this research is in Reynolds-Averaged Navier Stokes (RANS) methods. However, more research is heading in the direction of Large Eddy Simulations (LES). This transfer of interest is largely due to the rapid improvement in computing power, which makes LES simulations more feasible, as well as the desire to have time accurate simulations rather than just mean quantities and turbulence statistics, as provided by RANS simulations. Presented here for context is first a brief explanation of the physics of turbulence and then the hierarchy of turbulence models, based on the completeness of such physics included in each model. Of these models LES will then be discussed in more depth with specific emphasis on Wall-Modeled LES (WM-LES). Next, Shock Turbulent Boundary Layer Interactions (STBLI) will be discussed and finally, the current experimental and wall-resolved resolved computational efforts, of the same geometry selected for this study, will be presented.

2.1 Physics of Turbulence

Critical to understanding the modeling of turbulent flows is to have an understanding of the underlying physics of turbulence, of which these models are trying to represent. Two turbulent phenomena that are important to this study are the spectral representation of turbulence and the law of the wall.



Spectral Distribution.

Turbulence consists of a continuous spectrum of length and time scales in which energy is transfered successively from the largest of scales to the smallest as the turbulence decays, termed an energy cascade. The successively decreasing scales of turbulence can be classified into three general ranges. The first of these ranges consists of the largest scales where the majority of the energy is contained, and thus called the energy-containing range. Second, is the inertial subrange in which viscous effects are negligible and finally, the dissipation range where significant viscous effects are experienced and almost all of the dissipation occurs[8].

By using Fourier transforms and examining turbulence in wavenumber space one gains more insight into this energy cascade. Specifically, the Fourier transforms allow for the determination of which wavenumber, and equivalently, eddy size, contributes the most energy to the flow.

The inertial subrange and dissipation range make up the universal equilibrium range in which small-scale motions are statistically universal as hypothesized by Kolmogorov justified by the argument that as energy passes down the cascade all information about the direction and geometry of the large scale eddies is lost[8]. Thus, it is hypothesized that the energy spectra depends only upon the rate at which larger eddies supply energy, ϵ , and the kinematic viscosity, ν . Using dimensional analysis it was shown that the energy-spectrum as a function of wavenumber κ is then[15]:

$$E(\kappa) = C\epsilon^{2/3}\kappa^{-5/3} \tag{1}$$

The energy spectra, $E(\kappa)$, can be seen in terms of wavenumber, κ , in Figure 3 where the approximate locations of the three ranges are depicted. For homogeneous isotropic turbulence the power-law with energy-spectrum function exhibiting a slope of -5/3



can be clearly seen in Figure 3.



Figure 3. Energy spectrum for a turbulent flow.[3]

The Law of the Wall.

In a wall-bounded flow, the fluid's motion is restricted by the wall such that the viscous dissipation increases with ever decreasing scales of turbulence dictated by proximity to the wall[16]. It is found that the average shear stress is approximately constant from the wall throughout the boundary layer. This assumption allows for the derivation of the universal law of the wall, which is an empirically-determined description of how the mean streamwise velocity profile of a high Reynolds number turbulent boundary layer behaves near a wall. This velocity profile can be seen in Figure 4. One can see that there are three portions to this profile: the viscous sublayer, the log layer, and the defect layer. However, physically there are only two regions represented here: the inner and outer boundary layer, where the log layer represents the transition between the two[15].



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Figure 4. Typical velocity profile for a turbulent boundary layer.

This plot uses dimensionless parameters for velocity and height that are nondimensionalized by a velocity scale, which provides a universal relationship such that the profile can be compared between any Reynolds number and boundary layer thickness, defined as

$$u_{\tau} \equiv \sqrt{\frac{\tau_w}{\rho}} \tag{2}$$

where u_{τ} is known as the friction velocity, τ_w is the wall shear stress, and ρ is the local density. The dimensionless parameters for velocity, u^+ , and height, y^+ , are then defined as

$$u^+ \equiv \frac{u}{u_\tau} \tag{3}$$

$$y^+ \equiv \frac{u_\tau y}{\nu} \tag{4}$$



where u is the streamwise velocity, y is the height from the wall, and ν is the kinematic viscosity.

It is asserted that near the wall mean streamwise velocity is dependent only upon the wall shear, τ_w , the distance from the wall, y, and the fluid properties viscosity, μ , and density, ρ . A dimensional analysis yields the universal law of the wall as presented by Rotta as[16]:

$$u^{+} = F_1(y^{+}) \tag{5}$$

or

$$\frac{\partial u}{\partial y} = \frac{u_{\tau}}{y} F_2(y^+) \tag{6}$$

In the near-wall region the viscosity dominates and thus Equation (5) becomes

$$u^+ = y^+ \tag{7}$$

as shown in Figure 4. Away from the wall the viscosity contributes a negligible amount to the interaction of the mean flow and Reynolds stress carrying eddies and thus F_2 is simply a constant, $1/\kappa$, and Equation (6) can be integrated to the law of the wall presented as

$$u^+ = \frac{1}{\kappa} \ln y^+ + C \tag{8}$$

where κ is von Karman's constant found to be approximately 0.41 and C is an integration constant found to be approximately 5.0 from experiments conducted on flat plates[17].

A van Driest transformation can be applied to the velocity profile to allow comparison of a compressible flow to the incompressible law of the wall. The van Driest



transformation is provided by the following integration [18]:

$$u_{vD}^{+} = \int_{0}^{u^{+}} \sqrt{\frac{\rho}{\rho_w}} du^{+} \tag{9}$$

2.2 Hierarchy of Turbulence Modeling

To accurately describe turbulence one would have to use a Direct Numerical Simulation (DNS) in which the entire set of Navier-Stokes equations is solved and the entire set of physics is preserved for the flow. This would dictate the use of a grid that was discretized into elements small enough to resolve the smallest scales of turbulence leading to an extremely high number of grid points and therefore an extremely small allowable timestep. Specifically, the number of grid points needed to sufficiently resolve the smallest turbulent eddies scales as a function of $Re^{9/4}[9][12]$. To circumvent this issue, turbulence models are used to model the smaller scales, that require smaller grid spacing, in order to create a less-costly computation. The two major classes of turbulence models are Large Eddy Simulations (LES) and Reynolds-Averaged Navier-Stokes (RANS). LES models only the smallest of turbulent scales while fully including the physics of large scales and allows for time-dependent, or unsteady, calculations. RANS, on the other hand takes a temporal average of the entire flow. A helpful graphic depicting the hierarchy of turbulence modeling according to Blazek can be found in Figure 5[4]. In this graphic, Level 0 represents models which solve the full set of Navier-Stokes equations, simply DNS. Level 1 includes methods that model the smallest scales of turbulence, solely LES. Level 2 are second-order closures to include Reynolds-stress models and Level 3 are algebraic closures to RANS which are based on the eddy-viscosity hypothesis of Boussinesq[4].





Figure 5. Hierarchy of Turbulence Models[4].

2.3 Large Eddy Simulation (LES)

Large Eddy Simulations use the observation that small turbulent structures are more universal in character than large eddies[4] and that the large eddies carry the majority of the Reynolds stress[15]. Therefore, the larger energetic scales are calculated directly while the effects of the smaller energetic scales are modeled[4]. Graphically, one can see the energy spectrum of a turbulent flow in Figure 3 with the scales of the energy spectrum decreasing as the length scales decrease. One can also see rep-



resentative cutoff points of where certain models begin modeling the smaller scales. These subgrid-scale models allow for a reduction in grid resolution and thus LES can be applied at a Reynolds number an order of magnitude larger than DNS[4].

In boundary layer flows the energetic scales in the inner layer (approximately the inner fifth of the boundary layer) become increasingly smaller as the Reynolds number increases. This creates a "near-wall problem" in which smaller grid spacing is needed to fully resolve the flow near a wall to a point such that the wall-adjacent cell is under one wall unit $(y^+ \leq 1)[5]$. This increase in grid resolution leads to a need for a number of grid points approaching the cost of Direct Numerical Simulation (DNS)[12], thus limiting the Reynolds number that can be studied and greatly increasing the computational cost of simulations. To perform high Reynolds number LES simulations a CFD practitioner has several options, including: running simulations on full high-performance computers, running simulations at a fractional Reynolds number, under-resolving simulations, or wall-modeling.

Wall-Modeled LES.

To compensate for the "near-wall problem," wall-models are introduced which model the energetic eddies in the inner layer while still fully resolving the large-scale eddies found in the outer layer. These models correlate the velocity on the inner boundary of the outer layer to a single value of the wall shear stress[4]. Larsson et al. classify wall-models into two classes: those that use a hybrid LES/RANS method and those that use wall-stress models[12].

In the hybrid LES/RANS model LES computations are used above a certain threshold, between the inner and outer boundary layer, denoted by y_{int} while RANS is used below. Within hybrid LES/RANS there are two classifications of methods. The first is the models that maintain a fixed y_{int} during grid refinement and thus can



reach a grid-convergence state since the smallest resolved LES eddies will have a size proportional to y_{int} . The second classification within Hybrid LES/RANS includes models in which y_{int} is an interface location that is dependent on the grid and/or solution.[12]

Hybrid LES/RANS captures the large scale movement of energetic eddies unlike the completely RANS model, while using RANS to predict the attached boundary layer, in which it is well suited to do so. Hybrid RANS/LES has been successfully applied to flows such as injector ports and nozzles[19, 20, 21]. The disadvantages are that the energetic frequencies near the wall are lost. These small-scale eddies are critical to the dynamics near the wall and thus a better simulation is needed for resolving the shock turbulent boundary layer interactions of interest in hypersonic flows.

Once again Larsson et al. classifies the other class of wall-models, those that use wall-stress models, into two sub classes: models based on math or physical arguments[12]. The math-based models use control theory and filtering to assert mathematical arguments in order to predict wall stresses or slip velocity such as those of Nicoud et. al and Bose and Moin[22, 23]. The second class of wall-stress models use physics-based arguments, specifically momentum conservation in a nearly parallel shear flow such as those of Balaras et. al, Schumann, and Kawai and Larsson[24, 25, 26]. These physics based models assume either equilibrium, wherein the convection and pressure-gradient terms balance exactly, or non-equilibrium wherein all physics is accounted for[12]. Although Dawson et al. state that an equilibrium model may be insufficient for the flows of interest in this study, it has been shown that using a non-equilibrium model provided a prediction of skin friction that was no more accurate than an equilibrium model[27]. Larsson asserts that this is true because the LES itself treats 80% of the boundary layer and thus the wall-model is fed accurate



instantaneous information that captures the non-equilibrium effects of the flow[12]. Both an equilibrium and non-equilibrium wall-model will be studied in this research.

The current challenges of WM-LES are predicting separated and non-equilibirum flows as well as modeling multi-physics effects[12]. Recent successes of using WM-LES for a non-equilibrium flow have been documented by Park and Moin and for separated flow by Shur et. al[28, 29].

2.4 Mathematical Formulation

Navier Stokes.

The fundamental set of equations used for this simulation are the unsteady threedimensional Navier-Stokes equations. Written in divergence law form, the Navier-Stokes equations for one species are

$$\frac{\partial U}{\partial t} + \frac{\partial F_1}{\partial x_1} + \frac{\partial F_2}{\partial x_2} + \frac{\partial F_3}{\partial x_3} = 0$$
(10)

where U is the vector of conserved variables and F_j is a vector of fluxes in the x_j direction, as given below

$$U = \begin{pmatrix} \rho \\ \rho u_{1} \\ \rho u_{2} \\ \rho u_{3} \\ E \end{pmatrix}, F = \begin{pmatrix} \rho u_{j} \\ \rho u_{1} u_{j} + p \delta_{1j} - \sigma_{1j} \\ \rho u_{2} u_{j} + p \delta_{2j} - \sigma_{2j} \\ \rho u_{3} u_{j} + p \delta_{3j} - \sigma_{3j} \\ (E + p) u_{j} - \sigma_{kj} u_{k} - q_{j} \end{pmatrix}$$
(11)

wherein ρ is the density of the gas, u_j is the velocity in the x_j direction, p is the static pressure of the gas, δ_{ij} is the Kronecker delta, σ is the viscous stress tensor, E is the total specific energy, and q is the heat conduction vector[5].



The set of Navier-Stokes equations is closed through the use of an equation of state. For these experiments, a perfect gas is assumed and therefore the ideal gas law, given by equation (12), can be used as the equation of state.

$$p = \rho RT \tag{12}$$

This equation of state along with the definition of total enthalpy, specific gas constant, R, and ratio of specific heats, γ , allows a relationship for pressure to be written in terms of the primitive variables ρ , u_i , and E as given in equation (13).

$$p = (\gamma - 1)\rho \left[E - \frac{u_i u_i}{2} \right] \tag{13}$$

For a Newtonian fluid the viscous stress tensor, σ can be defined as

$$\sigma_{ij} = 2\hat{\mu}S_{ij} + \lambda \frac{\partial u_k}{\partial x_k} \delta_{ij} \tag{14}$$

where S_{ij} is the rate of strain tensor given by[30]

$$S_{ij} = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \tag{15}$$

and the bulk viscosity, λ , is taken according to Stokes hypothesis that:

$$\lambda = -\frac{2}{3}\mu\tag{16}$$

The heat flux vector, q_j , is given by Fourier's Law to be:

$$q_j = \hat{\kappa} \frac{\partial T}{\partial x_j} \tag{17}$$

The effective viscosity, $\hat{\mu}$, and effective thermal conductivity, $\hat{\kappa}$, are approximated using the Boussinesq approximation, which assumes a linear relationship between the



turbulent shear stress and the mean strain rate, therefore

$$\hat{\mu} = \mu + \mu_t \qquad \hat{\kappa} = \kappa + \kappa_t \tag{18}$$

where μ is the molecular component of viscosity, μ_t is the turbulent component of viscosity, κ is the molecular component of thermal conductivity, and κ_t is the turbulent component of thermal conductivity[5].

LES.

Large Eddy Simulations of compressible flows employ the use of both spatial filtering and Favre averaging along with the use of a Sub-Grid-Scale (SGS) model to achieve the aforementioned modeling of small scale turbulent fluctuations.

Spatial Filtering.

The premise of LES is that through the use of filtering the flow can be modeled with any flow variable, U, divided in to a filtered, \overline{U} , and sub-filter portion, U' where:

$$U = \overline{U} + U' \tag{19}$$

The filtered portion is the low-frequency turbulent eddies which are fully resolved while the sub-filter portion are the high-frequency turbulent eddies, which as previously discussed, are universal in character and are therefore modeled. The filtered variable is determined through the use of a low-pass filter with the form

$$\overline{U}(\vec{r}_0, t) = \int \overline{U}(\vec{r}, t) G(\vec{r}_0, \vec{r}, \Delta) d\vec{r}$$
(20)

where \vec{r} is the position in space and G is the filter function. The filter function, G, is a function of the difference in space $\vec{r}_0 - \vec{r}$ and the filter width Δ defined as



 $\Delta = (\Delta_1 \Delta_2 \Delta_3)^{1/3}$ where the subscripts denote each spatial direction[4].

The three most well known types of explicit filters are a Tophat, Fourier cut-off, and Gaussian. However, more commonly, filtering is done implicitly through the use of grid spacing along with the inherent discretization error of all calculations.

Favre Averaging.

Favre averaging, or density weighted averaging, is used when the density is not constant, such as compressible flows. This form of averaging provides a simplified set of equations while keeping the non-linear nature of the compressible form of the Navier-Stokes equations. Similarly to before the flow variable, U, is decomposed into a average quantity, \tilde{U} , and fluctuating portion, U'' where:

$$U = \tilde{U} + U'' \tag{21}$$

The averaged variable is given by[4]:

$$\tilde{U}(\vec{r}_0, t) = \frac{\overline{\rho U}}{\overline{\rho}} = \frac{1}{\overline{\rho}} \int \rho(\vec{r}, t) U(\vec{r}, t) G(\vec{r}_0, \vec{r}, \Delta) d\vec{r}$$
(22)

Wall-Model.

The wall-model developed by Komives will be implemented for this study[5]. This wall-model uses a reduced set of the Reynolds-Averaged Navier-Stokes in the modeled region to account for compressibility, heat transfer, and inertial effects. For the wall model the x_1 and x_2 directions are arbitrarily assigned orthogonal wall-tangent directions while x_3 is defined as wall-normal. Several key assumptions are made for the wall-model. First, the pressure in the wall-normal direction is assumed to be constant allowing for the decoupling of the conservation of wall-normal momentum and the conservation of mass from the full Navier-Stokes equation set. From the



equation of state equation (10) becomes [5]

$$\frac{\partial Q}{\partial t} + \frac{1}{\rho} \left[\frac{\partial G_1}{\partial x_1} + \frac{\partial G_2}{\partial x_2} \right] = 0$$
(23)

where

$$Q = \begin{pmatrix} u_1 \\ u_2 \\ e \end{pmatrix}, G_j = \begin{pmatrix} \rho u_1 u_j + p \delta_{1j} - \sigma_{1j} \\ \rho u_2 u_j + p \delta_{2j} - \sigma_{2j} \\ (E+p)u_j - \sigma_{kj} u_k - q_j \end{pmatrix}$$
(24)

In an equilibrium boundary flow it is assumed that the production and dissipation terms balance each other and the sum of the diffusive terms is zero. With these assumptions the equilibrium wall-model omits the convective and pressure gradients. When these assumptions are not made a non-equilibrium model is formed in which these convective and pressure gradients are included, through use of two inertial source terms[5]. In the non-equilibrium model the convective term is pulled from the probe location and Van Driest damping is employed to the wall. The convective term is turned off when there is a strong pressure gradient in the wall-tangential direction. This set of equations is suited for implicit solution and thus the solution strategy of Bond and Blottner is employed, in which the density field and flow primitives are updated in an outer loop while the remaining equations are solved in a decoupled fashion in an inner loop[31]. For further detail on the derivation of the wall-model see Appendix A of Reference [5].

This reduced set of equations is employed on a node-based mesh in the near wall region, where the outermost cell of the wall-model coincides with the probe location in the solver, as can be seen in Figure 6[32].

The probe location is taken to be several cells off the wall, as suggested by Kawai and Larsson, due to the inaccuracy of the first several cells off the wall[26].





Figure 6. Embedded wall-model grid showing probe location at 4 cells off the wall[5].

Eddy Viscosity Modeling.

The eddy viscosity model used for this wall model is a mixing length model with near-wall damping. This eddy viscosity model is chosen because it describes the eddy viscosity profile typical of the near-wall region of a boundary layer not subject to any pressure gradient, as assumed in the equilibrium wall-model. This method is completely local, requiring only local wall-shear, τ_w , density, ρ , and distance from the wall, x_3 , as given in Equation (25)

$$\mu_t = \rho \kappa x_3 \sqrt{\frac{\tau_w}{\rho}} D \tag{25}$$

with the damping function, D, defined as

$$D = \left[1 - e^{-(x_3^*/A^+)}\right]^2 \tag{26}$$

where, $A^+ = 17$, the von Karman constant, κ , is 0.41, and the wall coordinate, x_3 is modified to account for cold wall conditions to be x_3^* , given by:


$$x_3^* = x_3 \frac{\sqrt{\rho \tau_w}}{\mu} \tag{27}$$

Details of the development and basis for Eqs. (25)-(27) are given in reference [5].

2.5 STBLI

Shock Turbulent Boundary Layer Interactions (STBLI) occur when the boundary layer separates due to an adverse pressure gradient produced by a shock. These interactions create low-frequency oscillations in the shock position and therefore fluctuations in the pressure and density distributions of such a flow over an object of engineering interest[2]. Numerous experimental studies have been performed on a wide variety of shock turbulent boundary layer interactions, including both two-dimensional and three-dimensional interactions [33, 34, 35, 36, 7]. While a much smaller number of DNS or wall resolved LES has been performed on such flows [37, 38, 39, 40, 41]. Specifically within wall-modeled LES, the studies are largely only for two-dimensional flows 32, 27. For flows of engineering interest though the flows are more often threedimensional and thus more information is needed on how these wall-models handle three-dimensional flows such as fins, cylinders, and swept ramps 5. Adler et al. provides a comparison between computational efforts and experimental results of the STBLI of a swept-compression ramp[2]. The results look promising for two dimensions, and the intent of this study will be to assess predictions of wall-models for three-dimensional shock turbulent boundary layer interactions, such as that produced by a swept-compression ramp.



2.6 Geometry of Interest

The geometry of interest for producing three-dimensional STBLI is a sweptcompression ramp with 22.5° of compression and 30° of sweep. This specific geometry was chosen due to the availability of previous data from the wind-tunnel experiments of Vanstone et al. and the WR-LES of Adler et al.[2, 7]. While both of the aforementioned studies focus on analysis of the unsteady dynamics of the STBLI, the current study will focus more closely on the wall-model's ability to predict these unsteady phenomena. Further details of the computational and experimental studies will be discussed in Chapter 3.

The interactions seen in the different swept-compression-ramp configurations possess a conical symmetry in which the mean flow properties and frequency content converge to a virtual conic origin (VCO) when plotted in spherical coordinates. This means that the separation length grows linearly with displacement from this VCO, as seen in Figure 7[2].



Figure 7. Diagram of the collapse of separation, ramp corner, triple point, and reattachment to the VCO by Adler et al.[2]



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The Virtual Conic Origin (VCO) is expected to be at an x location of $-3.4/\delta_{99}$ and z location of $-5.8/\delta_{99}$, where x is the streamwise direction and z is the spanwise direction with the origin located at the upstream-ramp-corner[2].

In these three dimensional interactions the flow separation remains open and lowfrequency unsteadiness ($St_{\delta} \leq 0.01$) is not prominent[2]. Mid-frequency dynamics ($0.01 < St_{\delta} < 0.2$), however, are observed and are related to Kelvin-Helmholtz shedding from the separated shear layer near the separation line[2].



III. Methodology

The general CFD method begins with defining the geometry and flow of interest. This specified domain is then discretized to form a computational grid that covers both the surface and volume of interest. A simulation is then run using this grid and the desired numerics combined with the appropriate boundary conditions for the flow. From this simulation the results are verified and conclusions are drawn about the observed flow characteristics.

3.1 Previous Studies' Geometry and Flow Conditions

The geometry selected for study, in order to produce a three-dimensional shock turbulent boundary layer interaction, was a swept-ramp with a sweep angle of 30° and a compression angle of 22.5°. This specific ramp was chosen due to the availability of previous results from both experimental studies, of Vanstone et. al, and wall-resolved simulations, of Adler et. al[7, 2]. The aforementioned wall-resolved simulation of Adler et al. used a fractional Reynolds number to make the study tractable. The present study first ran simulations of this fractional Reynolds number in order to determine the wall-model's capability in predicting aerodynamic quantities as compared to a wall-resolved study. This study also includes simulations at the experimental Reynolds number to determine if large scale features of the interaction were captured in a fashion similarl to the fractional Reynolds number case. A second reason was to determine the capability of the wall-model in computing a high Reynolds number flow in a relevant amount of time. The flow conditions used for the original experimental study of Vanstone et al., the WR-LES of Adler et al. and the WM-LES of this study are presented in Table 1[7, 2]. All simulations were run using a perfect-gas assumption.



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Property	Vanstone et al. Experiment	Adler et al. WR-LES	Present Work WM-LES
M_{∞}	2.0	2.0	2.0
$U_{\infty}(m/s)$	510	510	510
$T_0(K)$	292 ± 5	292	292
$\delta_{99}(m)$	12.5×10^{-3}	12.5×10^{-3}	$12.5 imes 10^{-3}$
heta(m)	0.90×10^{-3}	0.90×10^{-3}	0.90×10^{-3}
Re_{δ}	4.75×10^5	1.62×10^4	$1.62 \times 10^4 \& 4.75 \times 10^5$
Re_{θ}	3.42×10^4	1.60×10^3	$1.60 \times 10^3 \& 3.42 \times 10^4$

Table 1. Experimental, WR-LES, and WM-LES flow properties.

3.2 Domain and Discretization

Domain.

The domain for this study, despite including a relatively simple geometry, was created in Solidworks 2016, a computer-aided design software, so that precise control of two specific features could be exercised. The first of these two features was at the downstream outflow domain. In order to promote orthogonality at this domain during grid smoothing it is desirable to incorporate a large fillet such that there are no sharp angles initiated by the ramp. The fillet ensures that the gridlines smoothly transition from perpendicular to the ramp to vertical. This fillet was created such that the circle was perpendicular to both the ramp plane and the horizontal top of the domain. The design of this fillet can be seen in Figure 8.

The second of these features was a baffle surface placed approximately four boundary layer thicknesses, 4δ , from the ramp wall. This was done so that a convergence study could be easily performed on the boundary layer spacing of the grid by creating a fixed distance that points could be spaced between in the wall-normal direction. A smooth baffle surface was chosen rather than a translated swept-ramp, again, in order to promote orthogonality during grid smoothing. This baffle surface can be seen in Figure 9.





Figure 8. Diagram of cross-section of domain, in the x-y plane, showing the fillet at the downstream outflow.

The domain started approximately 32 boundary layer thicknesses before the upstream ramp-corner in the x-direction such that the synthetic turbulent inflow, to be discussed later, had an adequate amount of time to equilibrate before the region of interest occurred. The domain then extends approximately 24 boundary layer thicknesses past the upstream-ramp corner in the x-direction to allow enough room for the interaction region followed by growth cells for dissipation. The top of the domain was fixed at a height of 0.3125m in the y-direction again to allow enough room for any pertinent interactions to occur along with growth cells for dissipation. The domain was a fixed width of 0.2125m in the spanwise z-direction, matching the wall-resolved study of Adler et. al, and providing adequate room for spanwise relief of the flow.





Figure 9. Diagram of domain showing the baffle surface 4δ above the wall, as depicted in blue.

Discretization.

WM-LES Grid.

To create the meshes used for the wall-modeled simulations Link3D and Pointwise were used conjointly to create block-structured meshes that were orthogonal, lowskew, and isotropic. GoHypersonic Inc.'s Link3D is a parallel-capable multi-block structured grid smoother purposely built for hypersonic research[42], while Pointwise is an all-purpose mesh generation software. As mentioned previously, in order to study grid convergence it was desired to have a fixed spacing between the wall and the baffle surface. To accomplish this a near-wall mesh was created in LINK3D that encompassed the volume from the wall to the baffle surface at 4δ above the wall. This grid was created such that orthogonality was achieved at each of the boundaries, including the baffle surface. The number of points in the wall-normal direction were then simply adjusted to achieve different grid spacing.

The spanwise and streamwise spacing was chosen to be small enough to resolve



turbulent structures in those respective directions, using the WR-LES grid of Adler et al. as an estimate of the number of cells needed[2]. These grid spacings also align with the best practices of the LES community, as prescribed by Georgiadis et. al, in which[43]:

$$50 \le \Delta x^+ \le 150 \qquad \qquad 15 \le \Delta z^+ \le 40 \tag{28}$$

with x as the streamwise direction and z as the spanwise direction. The values for this study are presented in Table 2.

Table 2. Grid spacing of WR-LES

Re_{δ}	Δx^+	Δz^+		
1.62×10^4	49	28		

To ensure grid independence, a grid with one-half the number of cells on the wall, and approximately 70% of the number of points in both the spanwise and streamwise direction, was created. The grid spacing in the streamwise direction was chosen such that equal spacing was achieved at the spanwise center of the grid, since the sweep of the ramp creates a difference in spacing on either side. Grid stretching was applied near the outflow in order to provide dissipation of any numerical errors that could be reflected back into the region of interest (the ramp corner).

The grid was then finished in Pointwise where hyperbolic tangent stretching was applied from 4δ to the top of the domain. The spacing of the first cell along the baffle in the wall-normal direction was chosen to match the fixed spacing within the lower region such that there was a smooth transition between the two blocks. The number of points in the wall-normal direction was fixed in this region creating slightly different grid stretching in this upper block between grids. Grid stretching was also applied near the top of the domain since it primarily consists of freestream properties



with no flow of interest as well as to dissipate any unphysical flow phenomena from returning to the region of interest. A cross-sectional view of one of these grids can be seen in Figure 10. Of note is that the same grid was used for both the wall-resolved Reynolds number cases and the experimental Reynolds number cases.



(a) Domain beginning at 20δ , displaying every 10th grid line

(b) Focus on ramp-corner

Figure 10. Cross-section of surface grid used in the WM-LES studies.

Grid	L_x	L_y	L_z	Δx	Δy	Δz	Δx^+	Δy^+	Δz^+	N_{total}
Coarse Medium Fine	$52\delta_{99}$ $52\delta_{99}$ $52\delta_{99}$	$25\delta_{99}$ $25\delta_{99}$ $25\delta_{99}$	$17\delta_{99}$ $17\delta_{99}$ $17\delta_{99}$	$\frac{\delta_{99}/20}{\delta_{99}/20}$	$\frac{\delta_{99}/30}{\delta_{99}/40}$	$\delta_{99}/32.5$ $\delta_{99}/32.5$ $\delta_{99}/32.5$	$49 \\ 49 \\ 49 \\ 49$	$\begin{array}{c} 60\\ 50\\ 40 \end{array}$	$28 \\ 28 \\ 28 \\ 28$	107M 129M 151M

Table 3. Grid Properties for wall-normal grid convergence study.

The total number of cells, N_{total} , is not a good comparison between the WR-LES and WM-LES grid size since different synthetic turbulence methods were used causing differences in the length of the inflow region. However, for the same spanwise and streamwise grid spacing as the WR-LES the WM-LES coarse, medium, and fine grids provided a 36%, 20%, and 4% reduction in wall-normal grid points, respectively.



DDES Grid.

Wall-resolved grids with wall-normal spacing under one wall unit $(y^+ \leq 1)$ were also created for use in Delayed Detached Eddy Simulation (DDES). Unlike before, two different grids were created for each of the Reynolds numbers to achieve the aforementioned condition at the wall. These grids were created entirely in Link3D with spanwise and streamwise spacing being the same as the wall-modeled grids but with grid clustering now in the wall-normal direction. The near-wall spacing was selected as to achieve a $y^+ = 1$ based on that grid's specified Reynolds number and a growth rate of 8% was applied away from the wall. The same grid stretching was applied near the downstream outflow and top of the domain A cross-sectional view of one of these grids can be seen in Figure 11.





3.3 Boundary Conditions

The wall boundary condition was chosen to match the experiment with an isothermal condition set at a fixed stagnation temperature provided from the experiment of



292K. The outflow and the ceiling of the test volume were set as supersonic outflows and the upstream-ramp-corner side was set as an adiabatic no-slip wall to simulate the placement of a fence within the experiment[2]. The downstream-ramp-corner boundary condition was originally selected to be a supersonic outflow; however, this led to increased separation due to the presence of spanwise reverse flow caused by the swept ramp. To fix this issue, a hybrid boundary condition was used as done by Adler et al.[2]. Any flow at the boundary with a positive spanwise velocity was treated with a supersonic outflow condition as before, but any flow with a negative spanwise velocity, thus an inflow, was treated with an adiabatic slip wall condition in which the spanwise velocity becomes zero. Finally, the inflow was treated with an artificial turbulent inflow. A diagram of the prescribed boundary conditions is found in Figure 12.



Figure 12. Boundary Conditions with x-y cross-section on the left and top down, x-z cross section on the right.

Turbulent Inflow.

To create the artificial turbulent inflow, the digital filtering technique of Kartha et. al was used[44]. In this method a two-dimensional RANS simulation of a flat-plate at the flow conditions of interest was first run. From this simulation, the streamwise position of the desired boundary layer thickness was found. A one-dimensional bound-



ary layer profile was then taken from a distance 30δ upstream from this location such that the inflow provides a boundary layer height that grows to the desired thickness near the separation. Inflow pertubatons of this profile were generated as to provide a time varying inflow with appropriate Reynolds stresses weighted for compressibility by the use of Morkovin scaling[5]. Both the normal and shear Reynolds stresses along the flat-plate portion of the domain were compared to the incompressible profile of DeGraaff and Eaton to determine whether the synthetically generated turbulence was equilibrated[6].

3.4 US3D

The analysis software used for this study was US3D version 1.0RC22, a finitevolume compressible Navier-Stokes solver extensively validated for hypersonic flows[45]. The numerical methods chosen for these studies, available in this tool, are discussed below.

LES.

For the LES simulations time advancement was done using 3rd Order Runge-Kutta time integration. Inviscid fluxes were evaluated using the kinetic-energy consistent scheme of Subbareddy and Candler at 2nd order for one flow time, to help initialize the flow from a free-stream with artificial boundary layer initial condition, before being increased to 6th order for the remainder of the simulation[46]. A Ducros sensor was used as a shock sensor. The Vreman model was used for subgrid-scale viscosity in the LES due to its availability in the software[47]. For wall-modeled cases the wall-model of Komives was used to provide corrected wall heat flux and skin friction to the LES calculation as detailed in Section 2.4[5].

The simulations were run without the use of the wall-model for the first two flow



times in order to initialize the turbulence needed for the wall-model assumptions. Once the wall-model was turned on the simulations were run for four flow times before mean statistics were collected for four flow times. Although this provided solutions in some variables that are visibly not converged, the statistics are deemed indicative enough to draw conclusions from.

DDES.

For the DDES simulations, 2nd order implicit Crank-Nicolson time integration with point relaxation was used. Inviscid fluxes were evaluated at 2nd order for one flow time as with the LES, but 4th order after that. Turbulence was modeled using Delayed Detached Eddy Simulation with the original Spalart-Allmaras model (SA-Catris)[13, 14].

3.5 Test Matrix

Grid Convergence.

Normally, to show grid convergence one must show that the results produced are independent of the grid. In the case of WM-LES there are two grids for which this must be proven true; the large scale LES grid as a whole and the one dimensional wall-model grid.

LES Grid.

As discussed previously the grid in the area of interest, approximately 4δ from the wall, has fixed spacing in the wall normal direction. To show grid convergence this spacing was varied with respect to the number of cells per boundary layer. Grids with wall normal spacing of $\delta/30$, $\delta/40$, and $\delta/50$ were used. Special care was used to ensure that the wall-model physical probe location stayed at approximately the



same location when pulling from each of these grids. A grid with one half the number of cells on the wall was also run to ensure grid independence in the streamwise and spanwise directions.

Wall-Model Grid.

With the location of the wall-model probe fixed, the density of the one-dimensional wall-model grid was varied to ensure grid independence within the wall-model. The medium density grid was run using three different numbers of wall-model points: 17, 35, and 60. The intermediate number of points, 35, leads to a wall-model z^+ of 1 for the first point in the wall-model and a wall-model z^+ within the log-layer at the probe location.

Wall-Model Flux Changes and DDES.

A DDES simulation was run at both the experimental and wall-resolved Reynolds numbers for use in comparing how other methods of handling high Reynolds numbers flows do in comparing the same interaction. The wall-modeled calculations were run using the medium density grid for three different flux schemes: an equilibrium model, one with the added pressure term, and one with convective fluxes added.

3.6 Comparisons

Comparisons were drawn between the wall-modeled LES and both the wall-resolved study of Adler et al. and the experiment of Vanstone et al.. Comparisons were also made to simulations run using Delayed Detached Eddy Simulation (DDES) using the Catris-Aupoix compressible formulation of the Spalart-Allmaras one-equation turbulence model[13][14].

Comparisons to the wall-resolved study of Adler et. al were done using mean



surface statistic line plots at several locations across the span to include lines at: 2δ , 4δ , and 8δ from the fence side. Comparisons of mean primitive variable contours were done at 4δ from the fence side. Surface streamlines plots were also compared for location of the VCO and finally power spectral density surrounding the interaction region was compared.

The same mean primitive variable contour plots were compared to particle image velocimetry (PIV) from the experiments. Surface streamlines were also compared to the oil flow visualization of the experiment.

Mean surface statistic line plots were used to compare values of aerodynamic properties to the DDES results. Once again, the surface streamlines were used to determine the location of the VCO. Conclusions were drawn on the ability of the wall-model to predict both aerodynamic quantities and the location of large scale interaction features.



IV. Results and Analysis

Before reporting the results of a Large Eddy Simulation, it is first important to show the computation's sensitivity to certain modeling parameters such as grid density, grid stretching, and boundary conditions[43]. For this study the sensitivity to grid density of the LES grid as well as the one-dimensional wall-model grid will be studied. The quality of the incoming turbulent statistics from the inflow boundary condition will be validated, the adiabatic wall temperature will be verified, and finally the appropriateness of the wall-model probe location will be determined.

4.1 Grid Independence Results

LES Grid.

To begin, the sensitivity of the LES grid to cell density was studied. Two different studies were completed; one combining the streamwise and spanwise directions along with one in the wall-normal direction. To determine the sensitivity of the solution to different grids, mean surface quantities, to include the three-directions of wall-shear and pressure, were compared at the midspan, approximately 8δ from the upstream ramp-corner side as shown by the line in Figure 13. When plotting data along this line the streamwise coordinate is normalized by the incoming boundary layer thickness $(\delta = 12.5 \times 10^{-3})$, with $x/\delta = 0$, $y/\delta = 0$, $z/\delta = 0$ located at the upstream-rampcorner.

Three LES grids were studied each with different wall-normal spacings between the ramp wall and a baffle surface approximately 4δ from the ramp wall. The coarsest of the grids had wall-normal spacing of $\delta/30$ which led to a y^+ between 70 and 150 across the wall. The medium density grid had wall-normal spacing of $\delta/40$ which led to a y^+ between 50 and 130. And, the finest of the grids had wall-normal spacing





Figure 13. Depiction of locations where the mean surface quantities are extracted from. Contour colors are of skin friction coefficient for a WM-LES simulation.

of $\delta/50$ which led to a y^+ between 20 and 120. The lower values occurred within the separation region and the flat-plate portion of the domain while the larger values occurred post-reattachment.

The results of this grid convergence study can be seen in Figure 14. One can see that while the $\delta/40$ and $\delta/50$ grids agree well the coarsest of the grids, $\delta/30$, varies more. The largest difference in values of shear in the x-coordinate is in the flat-plate portion of the domain where approximately a 2% difference between the fine and medium grids is seen while close to a 10% difference is seen between the coarse and fine grids. In the y-coordinate the greatest difference is seen in the minimum just after the ramp-corner. Between the fine and medium grids there is less than a 1% difference while between the coarse and fine grids there is a 30% difference. The



spanwise, z-direction, shear converges much slower than the other directions, and thus it is hard to determine the exact difference among the three. However, the coarsest grid does seem to predict values of τ_z lower than the medium and fine. The pressure is predicted the most closely among the three grids with less than a 1% difference between the fine, medium, and coarse grids. Since the $\delta/40$ and $\delta/50$ grids have a functionally insignificant difference in solutions the coarser of the two grids, $\delta/40$, was chosen for use in the rest of the simulations for computational efficiency.



(c) z-direction wall shear

(d) pressure normalized by freestream

Figure 14. Wall-normal grid convergence study mean surface quantities: $z = 8\delta$



After the computations sensitivity to wall-normal spacing had been determined the grid independence of the streamwise, x-coordinate, and spanwise, z-coordinate, spacing was verified. As mentioned previously the initial streamwise and spanwise spacings were chosen based on the wall-resolved study of Adler et al. as well as the suggested spacings of Georgiadis et al.[2, 43]. The results of this original grid spacing compared to a case with half the number of points on the wall, or approximately 70% of the points in each direction, can be seen in Figure 15.



Figure 15. Spanwise and streamwise grid convergence study mean surface quantities: $z=8\delta$



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Despite looking similar in profile there is a large difference between the two simulations. In the x-direction, the drop in shear occurs more rapidly and thus at approximately $x/\delta = -3.0$ there is a 35% difference in the value of x-direction wall shear. Similarly to the wall-normal convergence study, the largest difference in the y-direction wall shear occurs just after the ramp-corner. Between the full resolution grid and the half resolution grid there is a 32% difference in the minimum value. Again, due to slow convergence, it is tough to determine the exact difference of the z-direction shear between the two simulations but the half resolution grid does tend to be below that of the full resolution gird. And finally, the pressure values once again are very close with less than a 1% difference between the full and half resolution grids. Due to the large differences in predicted shears the full resolution grid is chosen for use in the remainder of the studies.

Wall-Model Grid.

With the determination that the medium density LES grid, $\delta/40$, with the spanwise and streamwise spacing of the wall-resolved study of Adler et al. is sufficiently resolved the sensitivity of the computation to the one-dimensional wall-model grid must be determined. Three different wall-model grid densities were used in simulations; one with 35 points which provided a wall-model $y^+ \approx 1.0$, one with half the number of points (17) which led to a $y^+ \approx 2.5$, and one with slightly less than double the number of points (60) which led to a $y^+ \approx 0.6$. The results of the wall-model grid convergence study are found in Figure 16.

One can see that all the solutions match very closely, especially within the region of interest from approximately 5δ to 10δ . The only discrepancy among the three is that the highest resolution wall-model, with 60 points, varies near the outflow in the three wall shear directions. Since this region is not of interest and the difference is





(c) z-direction wall shear (d) pressure normalized by freestream Figure 16. One-dimensional wall-model grid convergence study mean surface quantities: $z = 8\delta$

less than 20% at its largest the wall-models are deemed to be converged. The medium density wall-model grid, with 35 points, was chosen for use such that we maintain the desired condition that $y^+ \leq 1.0$ while not adding extra computational burden by adding additional points and thus calculations.



4.2 Wall-Model Probe Location

In addition to verifying that the one-dimensional wall-model has appropriate resolution one must also verify that the underlying assumption that the wall-model probe is placed within the log-layer is met. To do this, the dimensionless wall distance and van Driest transformed dimensionless velocity were extracted from the flow along the midspan 30 δ from the inflow, a point just before the separation region, and plotted as seen in Figure 17. The wall-model probe for this particular simulation was placed four cells from the wall as identified in Figure 17 by the circle. During simulations the y^+ of the probe location was recorded at each iteration and was found to match this point of approximately $y^+ = 5.6 \times 10^2$. Since this point does appear to fall within the log-layer, approximately $y^+ \leq 10^3$ for this location, it is deemed that this probe location fulfills the assumption of the wall-model.

4.3 Boundary Conditions

To assess the quality of the incoming turbulent statistics from the inflow boundary condition discussed previously the Reynolds shear and normal stresses in the pre-separation boundary layer were studied. A point along the midspan 30δ from the inflow was chosen for study and the Reynolds stresses were compared to the incompressible profile of DeGraaff and Eaton, with Markovin scaling for compressibility effects, in Figure 18[6]. The wall-normal and wall-tangential Reynolds normal stresses are predicted appropriately with no more than a 5% difference in the wall-tangential stress and very close prediction of the wall-normal stress before $y/\delta = 0.4$ of the wall. The discrepancy between the wall-normal stress after $y/\delta = 0.4$ is attributed to a compressible boundary layer being compared to an incompressible profile and the existence of the defect layer in this region. The Reynolds shear stress is also predicted with good agreement to the incompressible profile of Degraaff and Eaton with less





Figure 17. Log Layer matching of the LES grid with wall-model probe identified. The von Karman constant, κ , is 0.41 and the integration constant, C, is 5.1.

than a 10% difference in the near-wall region and less than 1% after that. With good agreement between these stress profiles, it can be asserted that the turbulence just upstream of the separation region is appropriately equilibrated and thus the synthetic turbulent inflow is suitable.

Another boundary condition of interest is the isothermal wall condition in which the adiabatic wall temperature was set. To check that this set temperature does produce an adiabatic wall the wall heating (from wall to fluid) can be seen in Figure 19. One can see that very small magnitudes, less than 1.0, are found indicating that this is an approximately adiabatic wall temperature, and appropriate for the study.

Now that several simulation factors such as grid density and the turbulent inflow have been validated for adequacy one can compare the simulations to the wall-resolved





Figure 18. Reynolds Stresses compared to incompressible profile of DeGraaff and Eaton[6].

and experimental studies with confidence that underlying errors are not creating any of the noted differences.

4.4 Equilibrium Wall-Model

Initially, an equilibrium wall-model was used based on the assertion by Larsson that a non-equilibrium model provided results that were no more accurate than a non-equilibrium model as discussed in Section 2.3[12]. The equilibrium model was first simulated at the Reynolds number of the wall resolved study of Adler et al. as to determine how a simulation with the assumptions of the wall model compares to a simulation which is not modeled at the wall, and therefore hypothetically the best that the wall-model could achieve in predicting the solution.

Virtual Conic Origin - Wall Resolved LES Reynolds Number.

When initially looking at the solution of the wall-modeled simulation at the wallresolved Reynolds number one can qualitatively tell that there is differences in the





Figure 19. Wall heating of $\delta/40$ WM-LES case

mean statistics when compared to the wall-resolved study of Adler et al.. These differences are especially clear when looking at surface streamtraces. The mean surface skin friction coefficient on the wall is displayed with these surface streamtraces in Figure 22. An obvious difference in the surface streamlines is noted with no streamwise reverse flow in the wall-modeled simulation. This lack of reverse flow allows for the separation front to move forward thus producing a different virtual conic than in the wall-resolved study. The wall-resolved study documented a virtual conic origin (VCO) at -3.4δ , -5.8δ in the x-z plane while the wall-modeled simulation produced a VCO at 0.79δ , 1.53δ . The virtual conic of the wall-modeled solution is visualized in Figure 21.





(a) Wall-Modeled LES (dashed line is ramp-corner)



(b) Wall-Resolved LES

Figure 20. Comparison of surface streamlines between WM-LES and WR-LES (z is up)[2].

Virtual Conic Origin - Experimental Reynolds Number.

The wall-modeled location of the virtual conic origin was also evaluated at the experimental Reynolds number. A similar result occurred with no streamwise reverse flow leading to a VCO at a location of $0.46\delta, 0.97\delta$ in the x-z plane. The WM-LES





Figure 21. Diagram depicting the collapse of the VCO for the equilibrium WM-LES (z is up).

streamtraces are compared to the oil flow visualization of the experiment in Figure 22. The data is presented with flow in the opposite direction in order to match the notation orientation of the experimental results. With qualitative differences in the mean surface flow the quantitative differences in mean flow properties were studied in order to gain more insight into the noted differences.



Figure 22. Comparison of surface streamlines between WM-LES and experiment (z is down)[7].



Mean Statistics.

The mean surface statistics were compared with data provided by Adler et al.. Again, the three-directions of wall shear as well as pressure were used as the quantities of interest with lines of data at several location across the span, to include; 2δ , 4δ , and 8δ from the fence. Several locations are compared so that the wall-model can be compared both in the highly reversed region near the fence boundary as well as at locations not in this region where there is no streamwise reverse flow. The comparisons of these lines can be seen in Figures 23 - 25.

Surface Quantities at Spanwise Location: $z = 2\delta$.

Near the fence-side boundary, at $z = 2\delta$, the largest differences are seen between the solutions of the WM-LES and the WR-LES. This is due to the equilibrium wallmodel predicting no streamwise reverse flow while the WR-LES predicts a strong reversal of flow that is almost two-dimensional in nature in this region. Before the interaction region, up to approximately $x = -2\delta$, all three directions of wall shear match closely between the WM-LES and the WR-LES. Of note, the spanwise wall shear of the WM-LES is slightly positive while the WR-LES value is slightly negative. The positive spanwise wall shear of the WM-LES is caused by the presence of a boundary layer on the fence boundary inducing a small spanwise velocity pre-shock. The difference between the two methods could be attributed to a difference in how the fence boundary condition was implemented. It is also likely that the difference can be attributed to the spanwise wall shear taking much longer to converge than the other directions, thus the difference is simply caused by unconverged statistics. This matching of undisturbed boundary layer values is a good calibration, showing that the wall-model is not erroneous in a simple flow.

In the streamwise, or x-coordinate, the WM-LES and WR-LES predict a drop in



wall shear at approximately $x = 2\delta$. The WR-LES predicts a larger and more abrupt drop in x-direction shear in which a mildly negative minimum value, corresponding to separation, is achieved just before $x = 0\delta$. This region of minimum shear lasts for approximately 1.5δ before increasing after reattachment at $x = 1.3\delta$. Comparatively the WM-LES predicts a more gradual drop in x-direction shear producing a separation region from $x = 0.5\delta$ to $x = 1.5\delta$. The reattachment locations agree quite well while the separation location of the WM-LES is well downstream of the WR-LES as seen in the surface streamlines. After the separation region both methods approach similar values from $x = 2\delta$ to $x = 4\delta$, with any small differences most likely due to unconverged statistics. Downstream of $x = 4\delta$ the WM-LES predicts values of x-direction wall shear 60% greater than the WR-LES. This difference is attributed to the increase in density after the shock creating larger values of y^+ in the WM-LES leading to an under resolved grid in this region.

In the y-direction, both the WM-LES and the WR-LES have an inflection point at the ramp-corner ($x = 1.1\delta$). While the WR-LES drops to a negative value almost imediately after the corner before taking a subsequent sharp increase the WM-LES remains positive. At $x = 2\delta$ the y-direction wall-shear, similarly to in the x-direction, converges to effectively the same values for both the WM-LES and the WR-LES up to $x = 4\delta$. As with the x-direction, the y-direction wall-shear of the WM-LES remains approximately 60% greater than the WR-LES for the remainder of the domain.

The largest differences between the WM-LES and the WR-LES are seen in the spanwise, or z-direction, wall shear. After the shock $(x = -2\delta)$ the spanwise wall shear of the WR-LES increases to values between $3 - 4 \times$ greater than the WM-LES. The spanwise statistics took much longer to converge than the other two directions. Thus, it is hard to discern relationships between peak values and separation flow features. However, it is important to note that the greater spanwise wall shear corresponds



to stronger crossflow within the separation region. Also of note is that the WM-LES has a relatively large negative value of wall-shear corresponding to negative crossflow, towards the fence boundary, while the WR-LES approaches values of 0, representing no spanwise flow. This again supports that there may be a difference in the implementation of the fence boundary. The normalized pressures agree well across the entire domain with less than a 10% difference, and good matching between the locations of the pressure rise due to the shock.



Figure 23. Comparison of mean surface statistics between WM-LES and WR-LES of Adler et al.: $z=2\delta$



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Surface Quantities at Spanwise Location: $z = 4\delta$.

The line of data at $z = 4\delta$ is just outside the highly reversed region of flow near the fence. Many of the same trends are seen as at $z = 2\delta$, but with less effect. In x-direction shear the WR-LES again drops to a value of minimum shear well below that of the WM-LES. This minimum of the WR-LES occurs at $x = 0.5\delta$ while the WM-LES minimum occurs just before $x = 1.0\delta$, a better agreement in location than at $z = 2\delta$. The separation region of the WR-LES lasts for 2.5δ before reattachment at $x = 2.9\delta$. Within this separation region the WR-LES exhibits a sharp increase in x-direction wall shear just before the ramp-corner at $x = 2.1\delta$ that recovers the same value of the WM-LES. The WM-LES predicts the region of low shear to begin just after the WR-LES at $x = 1.0\delta$ and last until 2.9δ . After reattachment the WR-LES and WM-LES again recover effectively the same values until $x = 6.5\delta$ in which the WM-LES predicts an x-direction wall shear 50% greater than the WR-LES for the remainder of the domain.

In y-direction wall shear an inflection point again occurs at the ramp-corner ($x = 2.1\delta$) with the WR-LES again dropping imediately. Contrary to at $z = 2\delta$ the WM-LES also drops slightly negative at the ramp-corner. However, this decrease is to a magnitude less than 10% of the WR-LES. Once again, just after reattachment at $x = 2.9\delta$ the WM-LES and WR-LES obtain effectively the same values until $x = 6.5\delta$.

In the z-direction the unconverged statistics again prevent any relationships to the separation features from being drawn. However, the values of spanwise wall shear were predicted slightly better at this location than at $z = 2\delta$ with the WR-LES values within the separation region only $1.5-2 \times$ larger than the WM-LES and values downstream of the separation of the same sign and within 20% of one another. Once again, good agreement is found between the normalized pressures.



Surface Quantities at Spanwise Location: $z = 8\delta$.

As predicted by looking at the surface streamline plots, the closest values of the mean surface quantities were found at the spanwise line the furthest from the fence. In the x-direction the wall shear reached a minimum for the WR-LES at $x = 1.9\delta$, approximately the same location where the WM-LES begins to plateau. Both the WM-LES and WR-LES predict an increase corresponding to reattachment at $x = 4.5\delta$. The WM-LES predicts a negative value of y-direction wall shear within 30% of the WR-LES and within the separation region the WM-LES predicts z-direction wall shear within 50% of the WR-LES. Despite being better than the other two locations these values are still quite different than the WR-LES. The one quantity that the WM-LES predicts an earlier pressure rise than the WR-LES by approximately one boundary layer thickness.





Figure 24. Comparison of mean surface statistics between WM-LES and WR-LES of Adler et al.: $z = 4\delta$





Figure 25. Comparison of mean surface statistics between WM-LES and WR-LES of Adler et al.: $z = 8\delta$



Contour Plots at Spanwise Location: $z = 4\delta$.

Along with the mean surface statistics mean cross-sectional contours were compared between the WM-LES and the WR-LES, at the lower Reynolds number of the WR-LES, to both qualitatively and quantitatively compare the structure of the interaction. The mean properties are plotted in a conical frame, using the upstream ramp-corner as the origin, with the polar coordinate, ϕ , being the angle from the x-z plane to the point of interest and the azimuthal coordinate, θ , representing the angle from the x unit vector to the point of interest. The mean solution of the WR-LES are mean properties averaged over both time and the radial coordinate while the WM-LES solution is a streamwise aligned slice averaged over only time. One can see these mean propety profiles in Figure 26 in which the color contours are the data of the WR-LES of Adler et al. and the dark contour lines are the data of the present study's WM-LES.

All of the mean contours match well in form while some vary slightly in value. The streamwise velocity, normalized by the freestream velocity, of the WM-LES has a slightly thicker boundary layer than that of the WR-LES leading to a slightly thicker separation bubble. The non-zero wall-normal velocity of the WM-LES protrudes farther from the ramp-corner than the WR-LES, this could be attributed to the larger separation produced by the thicker boundary layer, as is also the case with the density. The largest difference in values occurs in the pressures in which the pressures above the ramp of the WM-LES are approximately 25% lower than that of the WR-LES.

Mean contours of the three directions of velocity were also compared against the experimental particle image velocimetry (PIV) with the WM-LES performed at the experimental Reynolds number. These comparisons can be seen in Figure 27.

The same differences occur with the experimental data. The wall-model matches





Figure 26. Mean flow contours where lines are WM-LES and color contours are WR-LES of Adler et al.: $z = 8\delta[2]$.

the streamwise velocity well while the non-zero wall-normal velocities protrude further from the wall again. The wall-model also predicts stronger spanwise crossflow than the experiment within the separation region.




(c) w velocity normalized by u_{∞}

Figure 27. Mean flow contours where dashed lines are WM-LES and color contours are experimental PIV of Vanstone et al.[7].

Spectral Content.

The spectral content of the WM-LES was studied to compare the unsteadiness of the interaction with the reported results of the WR-LES. To study the spectral 57

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content the power spectral density (PSD) of pressure is taken from wall-adjacent cells at locations of interest throughout the flow. Upstream of the interaction region, a undisturbed turbulent boundary layer is present in which high-frequencies are normally present $(St_{\delta} \approx 1)$ [2]. One can see in Figure 28a that the WM-LES accurately predicts this with values of power spectral density (PSD) greatest surrounding 1.0. Between the separation and reattachment locations mid-frequency content ($0.01 \leq St_{\delta} \leq 0.2$), corresponding to Kelvin-Helmholtz (K-H) shedding is predicted[2]. Again the WM-LES predicts this accurately with large PSD values within this range as seen in Figure 28b and 28c. In three-dimensional interactions the K-H shedding also convects spanwise leading to less prominent contributions to the spectra downstream of the separation bubble. This is seen in Figure 28d by comparison of a point within the separation bubble and after reattachment. One can see that the point after reattachment has much smaller values of PSD within the mid-frequency range.





(c) Approximate reattachment point (d) Downstream of reattachment Figure 28. Spectral Data with PSD as a function of Strouhal number: $St_{\delta} = f\delta/U_{\infty}$

4.5 Non-Equilibirum Wall-Model

Despite close prediction in some areas of the flow the equilibirum wall-model fails in predicting reverse flow within the separation bubble leading to an inaccurate prediction of separation and reattachment location. Thus, the addition of the pressure term and then the pressure and convective fluxes in the wall-modeled set of equations was studied. These studies were originally done at the larger Reynolds number of the experiment and thus direct comparison to the wall-resolved study was not performed.



Virtual Conic Origin.

When looking at the mean surface flow with streamtraces one can see several notable features of the non-equilibirum wall-model, with both the pressure and convective terms included, as seen in Figure 29. The first is the presence of a secondary separation in which the flow abruptly turns at the beginning of the shock before reattaching and then separating again for the primary, and expected, separation region. This flow feature is not seen in the surface flow visualizations of either the WR-LES or experimental study. If the primary separation and reattachment are taken as the extents of the virtual conic, the VCO converges to a point at $-0.72\delta, -1.23\delta$ in the x-z plane. This produces a VCO which is closer to the expected location of $-3.4\delta, -5.8\delta$. This larger separation area is attributed to the presence of streamwise reverse flow unlike in the equilibirum wall-model. The secondary separation is attributed to the implementation of the wall-model across the shock. The wall-model assumes a constant pressure in the wall-normal direction which is not the case across the shock, thus creating a discrepancy in this region. This can be further evaluated by looking at mean contour plots of the flow.

Mean Statistics.

The mean statistics of the flow were also studied as before. The non-equilibrium wall-model takes much longer to converge so the mean profiles have much larger fluctuations to them than those of the equilibrium wall-model. The mean surface quantities are found in Figure 30. The non-equilibrium models present the secondary separation by a large fall in streamwise wall shear stress before recovering values that are slightly lower than that of the equilibrium model, but seem to recover negative values similar in trend to the WR-LES. The non-equilibrium model also produces a lower wall-normal shear stress, approximately $3 \times$ greater in magnitude than the





Figure 29. Diagram depicting the collapse of the VCO for the non-equilibrium WM-LES.

WM-LES, similar to the WR-LES. A higher spanwise shear stress is also seen similar to that of the WR-LES in which the WM-LES predicted values approximately 50% smaller within the separation region.

When observing the mean contours little difference is found between the mean quantities of the equilibrium and non-equilibrium wall-modeled solutions. This leads to the conclusion that this anomaly is not in the large scale resolved features but rather a non-physical product of the wall-modeled region. One quantity that does provide insight into the secondary vortex is the root mean square of the pressure fluctuations, p'_{RMS} . One can see the non-equilibrium wall-model spanwise contour compared to the wall-resolved contours in which both values have been normalized by the total





Figure 30. Comparison of mean surface statistics between non-equilibirum and equilibrium WM-LES: $z = 4\delta$

pressure. The non-equilibrium wall-model produces large pressure fluctuations at the foot of the shock, spanning this secondary separation area. This fluctuation across the shock suggest the need for the implementation of a shock sensor included in the wall-model to capture the unsteady shock foot.

Further analysis is still needed on how the mean values compare to the wallresolved study, at the same Reynolds number.



4.6 Comparisons to DDES

The wall-modeled simulations were also compared to the solutions of Delayed Detached Eddy Simulations (DDES) to compare the solution between the WM-LES and a popular method of computing high Reynolds number flows.

Virtual Conic Origin.

The surface flow visualization of the DDES is found in Figure 32. One can see that there is stronger reverse flow than predicted by the wall-model but also a secondary streamline convergence within the primary separation. The VCO converges to a point at -2.30δ , -0.45δ in the x-z plane.

Mean Statistics.

Since the DDES simulation was run at the experimental Reynolds number the shear quantities were non-dimensionalized by the freestream wall shear such that comparisons could be made to the wall-resolved study as well. These comparisons are found in Figure 33. One can see that for streamwise wall shear the DDES predicts values that are comparable to the lowest values of the wall-resolved study but occur at much different locations. The minimum value of the DDES occurs at $x = 2\delta$ while the WR-LES minimum value occurs nearly 2δ upstream just after $x = 0\delta$. While the WM-LES and WR-LES approach similar values after reattachment the DDES predicts values much lower. Of note is that the DDES does trend to a solution closer to that of the WM-LES nearly 60% greater than the WR-LES downstream of the reattachment. This shows that there may be an error upstream in the WR-LES. In the y-direction the DDES predicts a negative shear 50% larger than the WR-LES and again produces values 50% lower than the WR-LES and WM-LES post-reattachment. In the z-direction the DDES produces results that are similar to the WM-LES in



magnitude within the separation region but with a large spike in spanwise wall shear just before $x = 0\delta$ which corresponds to the secondary inflection of the crossflow as seen in the surface streamline plots. The pressure is predicted closely in value between the three simulations however the DDES predicts the pressure rise of the shock over a boundary layer thickness earlier than the other two methods.

Spectral Content.

When examining the differences between the spectral data of the WM-LES and the DDES one can see that the largest difference is the loss of high frequency content, as visible in Figure 34. This is because the DDES models more of the smaller scales, and equivalently the higher frequencies, of turbulence than an LES. However, the mid-frequency content corresponding to Kelvin-Helmholtz shedding is still present.

4.7 Computational Cost

The WR-LES of Adler et al. uses the aforementioned method of using a fractional Reynolds number to make the simulation of this flow tractable. The experiment was run at a Reynolds number of 4.75×10^5 while the WR-LES was run at a Reynolds number of 1.621×10^4 , approximately a factor of 29 smaller than the experimental value. At this fractional Reynolds number Adler et al. had an explicit timestep of $\mathcal{O}(10^{-8} - 10^{-9})$. At the same fractional Reynolds number the WM-LES could timestep at 1.0×10^{-7} , one to two orders of magnitude larger. This increase in allowable timestep allows for a much faster simulation with minimal added cost for the implementation of the wall-model.





(a) Root mean square of pressure fluctuations for the nonequilibrium wall-model.



Figure 31. Root mean square of pressure fluctuations for the wall-resolved study of Adler et al.[2].





Figure 32. Diagram depicting the collapse of the VCO for DDES.





Figure 33. Comparison of mean surface statistics between DDES, WM-LES and Wr-LES





(c) Approximate reattachment point

(d) Downstream of reattachment

Figure 34. Comparison of spectral data between DDES and WM-LES with PSD as a function of Strouhal number: $St_{\delta} = f \delta / U_{\infty}$



V. Conclusion

Summary.

A swept-compression ramp with 30° of sweep and 22.5° of compression was simulated using a wall-modeled large eddy simulation. The results of an equilibrium wallmodel were compared to the results of a wall-resolved large eddy simulation as well as an experiment, with matching Reynolds numbers for each. After the equilibrium wall-model failed to produce streamwise reverse flow the results of a non-equilibrium model were studied in comparison to the wall-resolved large eddy simulation. The non-equilibrium wall-model produced results which matched the values of certain flow properties of the wall-resolved study, such as wall shear, closer than the equilibrium wall-model did. However, a non-physical secondary separation was seen at the shock foot when using the non-equilibrium model.

Answers to Research Questions.

• Can a wall-modeled large eddy simulation adequately predict the dynamics of a three-dimensional shock turbulent boundary layer interaction?

Specifically:

- How does the location of flow features such as separation reattachment and virtual conic origin compare between the WM-LES, WR-LES, and experiment?
 - * When an equilibrium wall-model was used at the fractional Reynolds number of the wall-resolved study the virtual conic origin was found to be very different than that of the wall-resolved study. This is due to the lack of reverse flow predicted by the equilibrium wall-model



which fails to push the separation front farther upstream. When using a non-equilibrium wall-model more reverse flow was predicted but a non-physical secondary separation was observed, not seen in the WR-LES or experimental study. The equilibrium model at the higher Reynolds number of the experiment provided a similar result to the lower Reynolds number situation in which the virtual conic origin was within the domain due to the lack of reverse flow.

- How do mean flow quantities compare between the WM-LES, WR-LES, and experiment?
 - * The predictions of an equilibrium wall-model at the lower Reynolds number of the wall-resolved study were strongly dependent on the distance from the fence boundary condition. Near the fence WM-LES predicted values of streamwise and wall-normal shear that were much higher than the WR-LES study with no reversal in either of these directions. While in the spanwise direction the shear of the WM-LES was predicted to be less than half of what the WR-LES predicted. Further from the wall the values of wall shear were much closer, leading to a peak difference in skin friction coefficient of less than 15% between the WM-LES and the WR-LES. This led to much better alignment of both the separation and reattachment locations. A non-equilibrium model led to closer results of wall shear. In both the streamwise and wall-normal direction reverse flow was predicted and in the spanwise direction the shear was twice as large, similar to the WR-LES comparison at the lower Reynolds number.
- What is the savings in computational time between the WM-LES and WR-LES?



- In comparison to the WR-LES of Adler et al. the WM-LES was able to be run on a grid with a 20% decrease in wall-normal grid points. This increase in cell size allowed for the use of a timestep two orders of magnitude greater than the WR-LES leading to a net computational time decrease of approximately 10×.
- How do the WM-LES and WR-LES compare to simulations run using a hybrid RANS/LES method such as Delayed Detached Eddy Simulation?
 - A simulation run using DDES provided a VCO closer to that of the WR-LES but the separation was much farther ahead, which is expected of a DDES. The DDES was able to predict streamwise reverse flow present near the fence. However, a non-physical inflection point in the streamlines is seen within the separation as well as an area of recirculation present near the fence not seen in either the wall-resolved or experimental studies. The DDES provided values of minimum and maximum mean wall shear that were closer to the WR-LES, but occurred at different locations.

Significance of research.

This is one of very few studies that has evaluated the use of a wall-modeled large eddy simulation in predicting three-dimensional STBLIs. This study provides preliminary results of both an equilibrium and non-equilibrium wall-modeled large eddy simulation in use on a three-dimensional shock turbulent boundary layer interaction.

Conclusion.

The equilibrium wall-model is inappropriate for modeling an interaction of this type in which there is a strong reversal of flow. In an interaction without reverse flow the equilibrium model may be more appropriate for use. The non-equilibrium



wall-model predicted more appropriate quantities for reverse flow but provided a non-physical secondary separation. For a three-dimensional interaction the nonequilibrium model seems to be the more appropriate choice for capturing the flow features. A hybrid LES/RANS method was capable of predicting some flow features more accurately than both models to include the presence of streamwise reverse flow and and closer minimum and maximum values of wall shear. However, DDES provides a very different collapsing of the conic in comparison to the wall-resolved study with the length of the separation region being much longer for the majority of the span. The non-equilibrium model looks to be the most promising in accurately predicting three-dimensional interactions pending improvement of the model in the unsteady shock foot region. The inclusion of both the pressure and convective terms led to improved predictions of the separation and reattachment location across the span, as well as better predictions of mean wall shear.

Future research.

After seeing promising results from the non-equilibrium wall-model it is recommended that further research be done to investigate the cause of the non-physical secondary separation at the shock. If this apparent discrepancy can be resolved the non-equilibrium wall-model may provide very good results in comparison to a wallresolved study of the swept compression ramp.

The other area of interest would be to evaluate both the equilibrium and nonequilibrium wall-model in several other geometries that produce three-dimensional dynamics such as a fin or corner flow in order to determine where they are appropriate.



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